

**MABOPANE AND
WINTERVELD PLC**

GRADE 11

**MARKING GUIDELINES
MATHEMATICS: CONTROL TEST
(TERM 1)
24 MARCH 2026**

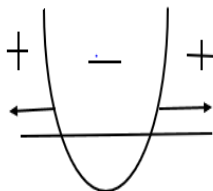
MARKS: 75

This marking guidelines consists of 10 pages

NOTE:

- If a candidate answers a question TWICE, mark only the FIRST attempt.
- Consistent accuracy applies in ALL aspects of the marking memorandum. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

QUESTION 1

<p>1.1.1</p>	$x(x - 2) + 7(x - 2) = 0$ $(x + 7)(x - 2) = 0$ $x = -7 \text{ or } x = 2$	<p>✓ factors</p> <p>✓ $x = -7$</p> <p>✓ $x = 2$</p>	<p>(3)</p>
<p>1.1.2</p>	$5x^2 + 2x - 6 = 0$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{-2 \pm \sqrt{(2)^2 - 4(5)(-6)}}{2(5)}$ $x = 0.91 \text{ or } x = -1.31$ <div style="border: 1px solid black; padding: 5px; margin: 10px auto; width: fit-content;"> <p>NOTE: Penalise 1 mark if the rounding off to TWO decimal places is incorrect</p> </div>	<p>✓ correct substitution into correct formula</p> <p>✓ $x = -0.91$</p> <p>✓ $x = -1.31$</p>	<p>(3)</p>
<p>1.1.3</p>	$15x - 4 < 9x^2$ $-9x^2 + 15x - 4 < 0$ $(3x - 1)(3x - 4) > 0$ <p>CV's: $x = \frac{1}{3}$ or $x = \frac{4}{3}$</p>  $x < \frac{1}{3} \text{ or } x > \frac{4}{3}$	<p>✓ standard form</p> <p>✓ both critical values</p> <p>✓✓ answer</p>	<p>(4)</p>

<p>1.1.4</p>	$9^x + 9 = 10 \cdot 3^x$ $3^{2x} - 10 \cdot 3^x + 9 = 0$ <p>Let $k = 3^x$</p> $k^2 - 10k + 9 = 0$ $(k - 1)(k - 9) = 0$ $k = 1 \text{ or } k = 9$ $\therefore 3^x = 3^0 \text{ or } 3^x = 3^2$ $\therefore x = 0 \text{ or } x = 2$ <p>OR</p> $9^x + 9 = 10 \cdot 3^x$ $3^{2x} - 10 \cdot 3^x + 9 = 0$ $(3^x - 1)(3^x - 9) = 0$ $3^x = 1 \text{ or } 3^x = 9$ $\therefore 3^x = 3^0 \text{ or } 3^x = 3^2$ $\therefore x = 0 \text{ or } x = 2$	<p>(5)</p> <ul style="list-style-type: none"> ✓ standard form ✓ k-method ✓ factors ✓ both answers of k ✓ answer OR ✓ standard form ✓ factors ✓ both answers for x ✓ prime number base ✓ answer <p>(5)</p>
<p>1.2</p>	$\frac{x}{2} + \frac{3}{2}y = 1 \dots\dots\dots (1)$ $y^2 + x = xy + y \dots\dots\dots (2)$ <p>$x = 2 - 3y \dots\dots\dots (3)$ from equation (1)</p> <p>Subt (3) into (2)</p> $y^2 + (2 - 3y) = (2 - 3y)y + y$ $y^2 + 2 - 3y = 2y - 3y^2 + y$ $3y^2 + y^2 - 3y - 2y - y + 2 = 0$ $4y^2 - 6y + 2 = 0$ $2y^2 - 3y + 1 = 0$ $(2y - 1)(y - 1) = 0$ $y = \frac{1}{2} \text{ or } y = 1 \dots\dots\dots (4)$ <p>Subt (4) into (3)</p> $x = \frac{1}{2} \text{ or } x = -1$ $\left(\frac{1}{2}; \frac{1}{2}\right) \text{ and } (-1; 1)$	<p>(6)</p> <ul style="list-style-type: none"> ✓ $x = 2 - 3y$ ✓ subst in (2) ✓ standard form ✓ factors ✓ values of y ✓ values of x

1.3	$x = \frac{4 \pm \sqrt{16 - 4m(-m+5)}}{2m}$ $16 - 4m(-m + 5) < 0$ $m^2 - 5m + 4 < 0$ $(m - 4)(m - 1) < 0$ $CV's: m = 4 \text{ or } m = 1$ $1 < m < 4$	<ul style="list-style-type: none"> ✓ $\Delta < 0$ ✓ standard form ✓ factors ✓ critical values ✓ answer 	(5)
			[26]

QUESTION 2

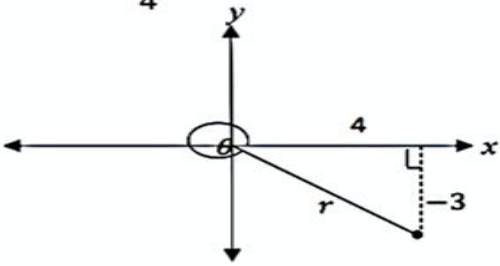
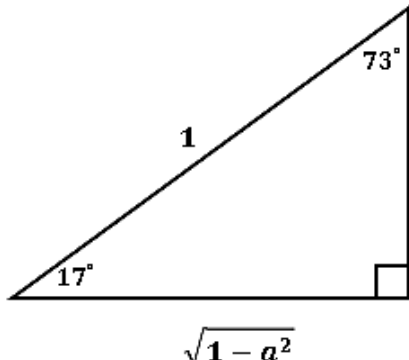
2.1	$A = xy$ $A = x(100 - 2x)$ $A = 100x - 2x^2$ $A = -2x^2 + 100x$	<ul style="list-style-type: none"> ✓ $A = x(100 - 2x)$ ✓ distributing x 	(2)
2.2	$A = -2x^2 + 100x$ $A = -2(x^2 - 50x)$ $A = -2\left(x^2 - 50x + \left(\frac{50}{2}\right)^2 - \left(\frac{50}{2}\right)^2\right)$ $A = -2(x^2 - 50x + 625 - 625)$ $A = -2[(x - 25)^2 - 625]$ $A = -2(x - 25)^2 + 1250$ <p>\therefore The maximum area is 1250 m</p>	<ul style="list-style-type: none"> ✓ method of completing the square ✓ $A = -2[(x - 25)^2 - 625]$ ✓ $A = -2(x - 25)^2 + 1250$ ✓ answer 	(4)
			[6]

QUESTION 3

<p>3.1.1</p>	$64^{-\frac{2}{3}}$ $= (2^6)^{-\frac{2}{3}}$ $= 2^{-4}$ $= \frac{1}{16}$ <p>OR</p> $= (4^3)^{-\frac{2}{3}}$ $= 4^{-2}$ $= \frac{1}{16}$ <p>OR</p> $= \frac{1}{64^{\frac{2}{3}}}$ $= \frac{1}{\sqrt[3]{64^2}}$ $= \frac{1}{4^2}$	$\checkmark (2^6)^{-\frac{2}{3}}$ $\checkmark 2^{-4}$ $\checkmark \frac{1}{16}$ <p>OR</p> $\checkmark (4^3)^{-\frac{2}{3}}$ $\checkmark 4^{-2}$ $\checkmark \frac{1}{16}$ <p>OR</p> $\checkmark \frac{1}{64^{\frac{2}{3}}}$ $\checkmark \frac{1}{\sqrt[3]{64^2}}$ $\checkmark \frac{1}{16}$	<p>(3)</p> <p>(3)</p> <p>(3)</p>
<p>3.1.2</p>	$\frac{3^{2n+2} - 9^{n-1}}{2 \cdot 3^{2n+1}}$ $= \frac{3^{2n+2} - 3^{2(n-1)}}{2 \cdot 3^{2n+1}}$ $= \frac{2 \cdot 3 \cdot 3^{2n}}{3^{2n+2} - 3^{2n-2}}$ $= \frac{2 \cdot 3 \cdot 3^{2n}}{3^{2n} \cdot 3^2 - 3^{2n} \cdot 3^{-2}}$ $= \frac{2 \cdot 3 \cdot 3^{2n}}{3^{2n}(3^2 - 3^{-2})}$ $= \frac{6 \cdot 3^{2n}}{6 \cdot 3^{2n}}$ $= \frac{9 - \frac{1}{9}}{6}$ $= \frac{80}{9} \times \frac{1}{6}$ $= \frac{40}{27}$	$\checkmark \text{exponential laws (base 3)}$ $\checkmark \text{common factor}$ $\checkmark \text{simplification}$ $\checkmark \text{answer}$	<p>(4)</p>

<p>3.1.3</p>	$\left(\frac{\sqrt{7^{2011}} - \sqrt{7^{2009}}}{\sqrt{7^{2008}}} + \sqrt{7}\right)^2$ $= \left(\frac{\sqrt{7^{2008}}(\sqrt{7^3} - \sqrt{7^1})}{\sqrt{7^{2008}}} + \sqrt{7}\right)^2$ $= (\sqrt{7^3} - \sqrt{7^1} + \sqrt{7})^2$ $= (7\sqrt{7} - \sqrt{7} + \sqrt{7})^2$ $= (6\sqrt{7} + \sqrt{7})^2$ $= (7\sqrt{7})^2$ $= 343$ <p>OR</p> $\left(\frac{\sqrt{7^{2011}} - \sqrt{7^{2009}}}{\sqrt{7^{2008}}} + \sqrt{7}\right)^2$ $= \left(\frac{7^{\frac{2011}{2}} - 7^{\frac{2009}{2}}}{7^{\frac{2008}{2}}} + \sqrt{7}\right)^2$ $= \left(\frac{7^{\frac{2009}{2}}(7-1)}{7^{1004}} + \sqrt{7}\right)^2$ $= (7^{\frac{1}{2}}(6) + \sqrt{7})^2$ $= (7\sqrt{7})^2$ $= (49)(7)$ $= 343$	<p>✓ $\sqrt{7^{2008}}$</p> <p>✓ $(\sqrt{7^3} - \sqrt{7^1})$</p> <p>✓ $7\sqrt{7}$</p> <p>✓ $(7\sqrt{7})^2$</p> <p>✓ answer</p> <p>OR</p> <p>✓ $7^{\frac{2009}{2}}(7-1)$</p> <p>✓ $(7-1)$</p> <p>✓ $7^{\frac{1}{2}}$</p> <p>✓ $(7\sqrt{7})^2$</p> <p>✓ answer</p>	<p>(5)</p> <p>(5)</p> <p>[12]</p>
--------------	---	--	-----------------------------------

QUESTION 4

<p>4.1.1</p>	<p>$\tan \theta = -\frac{3}{4}$</p>  <p>$r^2 = (4)^2 + (-3)^2$ Pythagoras $r^2 = 25$ $\therefore r = 5$ $\therefore \sin \theta = -\frac{3}{5}$</p>	<p>✓ diagram with values ✓ value of r ✓ answer $\sin \theta$</p>	<p>(3)</p>
<p>4.1.2</p>	<p>$\cos (180^\circ - \theta)$ $= -\cos \theta$ $= -\frac{4}{5}$</p>	<p>✓ $-\cos \theta$ ✓ answer</p>	<p>(2)</p>
<p>4.2</p>			
<p>4.2.1</p>	<p>$\sin 17^\circ = \frac{a}{1}$ $x^2 = (1)^2 - (a)^2$ $\therefore x = \sqrt{1 - (a)^2}$ $\tan 17^\circ = \frac{a}{\sqrt{1 - a^2}}$</p>	<p>✓ substitution pyth ✓ value of x ✓ answer</p>	<p>(3)</p>
<p>4.2.2</p>	<p>$\sin 107^\circ = \sin (90^\circ + 17^\circ)$ $= \cos 17^\circ$ $= \sqrt{1 - a^2}$</p>	<p>✓ $\cos 17^\circ$ ✓ answer</p>	<p>(2)</p>

	<p>OR</p> $\sin 107^\circ$ $= \sin(180^\circ - 73^\circ)$ $= \sin 73^\circ$ $= \sqrt{1 - a^2}$	<p>OR</p> $\checkmark \sin 73^\circ$ $\checkmark \text{answer}$	(2)
4.2.3	$\cos^2 253^\circ + \sin^2 557^\circ$ $= [\cos(180^\circ + 73^\circ)]^2 + [\sin(180^\circ + 17^\circ)]^2$ $= (-\cos 73^\circ)^2 + (-\sin 17^\circ)^2$ $= (-a)^2 + (-a)^2$ $= 2a^2$	$\checkmark -\cos 73^\circ)^2$ $\checkmark -\sin 17^\circ$ $\checkmark \text{method}$ $\checkmark \text{answer}$	(4)
			[14]

QUESTION 5

5.1.	$\frac{\cos(-180^\circ - x) \cdot \tan(360^\circ - x) \cos^2(90^\circ - x)}{\sin(180^\circ - x) \cdot \sin x}$ $= \frac{\cos[-(180^\circ + x)] \cdot \tan(360^\circ - x) \cos^2(90^\circ - x)}{\sin(180^\circ - x) \cdot \sin x}$ $= \frac{\cos(180^\circ + x) \cdot \tan(360^\circ - x) \cos^2(90^\circ - x)}{\sin(180^\circ - x) \cdot \sin x}$ $= \frac{-\cos(x) \cdot (-\tan x) \cdot \sin^2(x)}{\sin(x) \cdot \sin x}$ $= \frac{\cos(x) \cdot \tan x \cdot \sin^2(x)}{\sin^2(x)}$ $= \frac{\cos(x) \cdot \frac{\sin x}{\cos x} \cdot \sin^2(x)}{\sin^2(x)}$ $= \sin x$	$\checkmark -\cos(x)$ $\checkmark -\tan x$ $\checkmark \sin^2(x)$ $\checkmark \sin x$ $\checkmark \frac{\sin x}{\cos x}$ $\checkmark \text{answer } (\sin x)$	(6)
------	---	---	-----

<p>5.2</p>	$\frac{\sin x}{1 + \cos x} = \sqrt{\frac{1 - \cos x}{1 + \cos x}}$ <p>RHS:</p> $= \sqrt{\frac{1 - \cos x}{1 + \cos x}}$ $= \sqrt{\frac{(1 - \cos x)}{1 + \cos x} \times \frac{(1 + \cos x)}{(1 + \cos x)}}$ $= \sqrt{\frac{1 - \cos^2 x}{(1 + \cos x)^2}}$ $= \sqrt{\frac{\sin^2 x}{(1 + \cos x)^2}}$ $= \frac{\sqrt{\sin^2 x}}{\sqrt{(1 + \cos x)^2}}$ $= \frac{\sin x}{1 + \cos x}$ <p>RHS = LHS</p>	<p>(5)</p> <ul style="list-style-type: none"> ✓ multiply by: $\frac{(1 + \cos x)}{(1 + \cos x)}$ ✓ $1 - \cos^2 x$ ✓ $\sin^2 x$ ✓ simplify roots: $\frac{\sqrt{\sin^2 x}}{\sqrt{(1 + \cos x)^2}}$ ✓ answer
<p>5.3</p>	$3 \cos^2 x - 5 \sin x = 1$ $3(1 - \sin^2 x) - 5 \sin x = 1$ $-3 \sin^2 x + 3 - 5 \sin x - 1 = 0$ $-3 \sin^2 x - 5 \sin x + 2 = 0$ $3 \sin^2 x + 5 \sin x - 2 = 0$ $(3 \sin x - 1)(\sin x + 2) = 0$ $3 \sin x = 1 \text{ or } \sin x = -2$ $\sin x = \frac{1}{3} \text{ or } \sin x = -2$ <p>ref <'s,</p> $x = \sin^{-1}\left(\frac{1}{3}\right) = 19.47^\circ \text{ or } x \neq \sin^{-1}(-2) \text{ N.A}$ <p>I. $x = 19.47 + k.360^\circ, k \in \mathbb{Z}$</p> <p>II. $x = 180^\circ - 19.47^\circ + k.360^\circ, k \in \mathbb{Z}$</p> $x = 160.53^\circ + k.360^\circ, k \in \mathbb{Z}$	<p>(6)</p> <ul style="list-style-type: none"> ✓ $1 - \sin^2 x$ ✓ standard form ✓ $\sin x = \frac{1}{3} \text{ or } \sin x = -2$ ✓ ref <'s with rejection ✓ solution 1 ✓ solution 2
		<p>[17]</p>

TOTAL = 75 MARKS

ANALYSIS GRID (GRADE 11 TERM 1 TEST: 24 MARCH 2026)

Q.no	Concepts	Level 1	Level 2	Level 3	Level 4	Total
1.1.1	Solving by factorisation	3				3
1.1.2	Solving by quadratic formula	3				3
1.1.3	Inequalities		4			4
1.1.4	Exponential equation		5			5
1.2	Simultaneous equations		6			6
1.3	Nature of roots			5		5
Total		6	15	5	0	26
2.1	Area of a rectangle	2				2
2.2	Application of quadratic equations			4		4
Total		2	0	4	0	6
3.1.1	Laws of exponents	3				3
3.1.2	Exponents with fractions		4			4
3.1.3	Simplification of surds			5		5
Total		3	4	5	0	12
4.1.1	Terminal Arm		3			3
4.1.2	Reducing trig ratio		2			2
4.2.1	Trig ratio in term of a letter		3			3
4.2.2	Trig ratio in term of a letter		2			2
4.2.3	Numerical Reductions		4			4
Total		0	14	0	0	14
5.1	Reduction formula			6		6
5.2	Proving Identities			5		5
5.3	General solutions			6		6
Total		0	0	17	0	17
Gr.Total		11	33	31	0	75
Expected marks(policy)		15	26,25	22,5	11,25	75
Actual %		14,67%	44%	41,33%	0%	100
Expected(policy) %		20%	35%	30%	15%	100